# Conformational Properties of polypeptide chains

Chapter 5
Proteins
TE Creighton

#### Conformations

- For small molecules the calssical representations are sufficient.
- Their 3D structure is easy to determine by the bond length and angles.
- Larger polymers such as Proteins can have non interconvertible 3D conformations.
- Different conformations must have the same configuration of atoms.
- Polymers are very flexible and can have a large number of conformations.

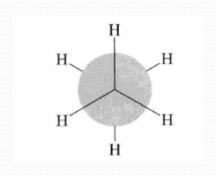
#### Conformations

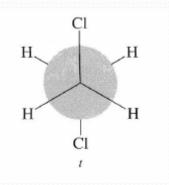
- Proteins:
- Have used this flexibility to adopt a number of fixed conformations.
- Protein structures do have a hierarchy:
- Primary structure- covalent structure of the amino acids.
- Secondary structure- local conformation of the polypeptide backbone.
- Tertiary and quarternary structure- 3D conformation of secondary structures and superstructures.

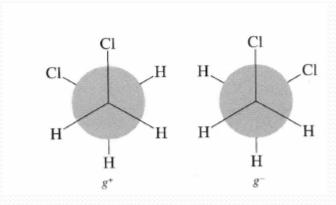
#### **3D Conformations**

- How a conformation is defined is not trivial
- Even a small molecule can seem to have an infinite number of conformations.
- Only conformations that have an energetic minimum are considered as stable conformations.
- Representations are shown in Newman projection

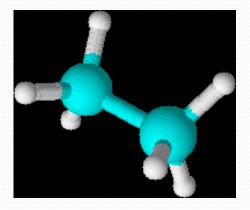
### **3D Conformations**



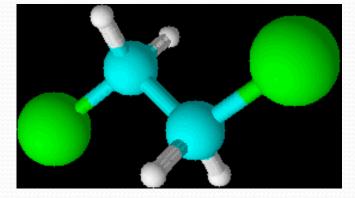


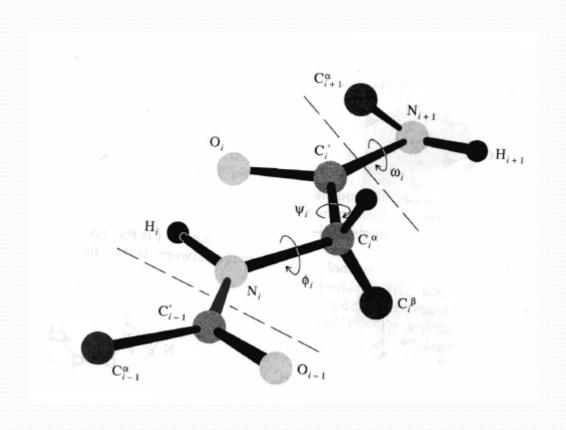


Ethane

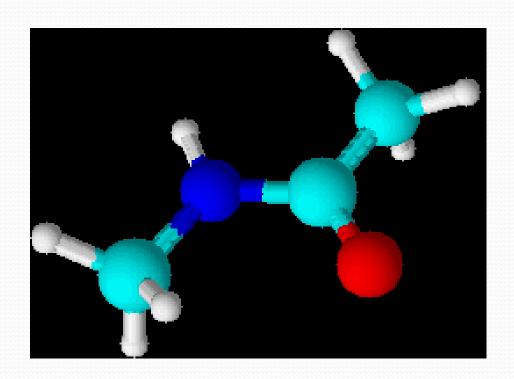


1,2 Dichloro etane





• The peptide Bond: Is normally planar

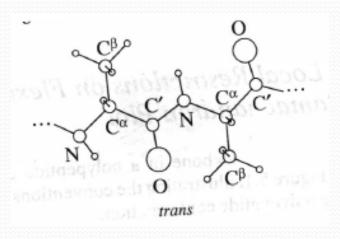


- The angles are callet Tau, describing the angles between  $NC^{\alpha}C'$
- Rotations about bonds are described as torsion or dihedral angles
- They are in the range -180 +180 degrees

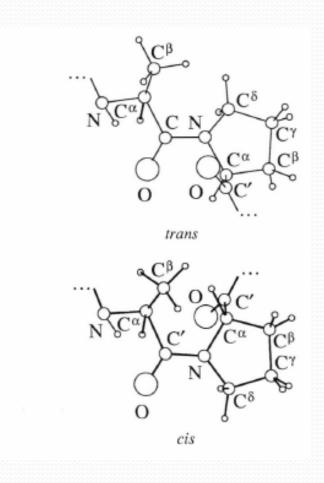
In trans conformation the angle is 180 deg, in cis conformation the angle is 0 deg.

Rotation around this bond: angle + value → rotation clockwise

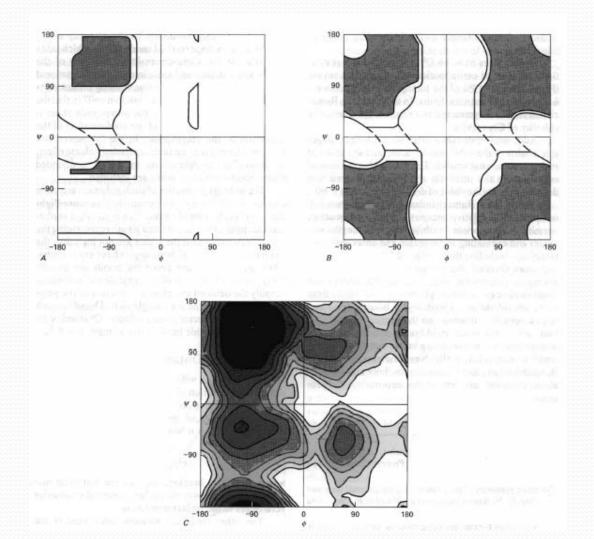
Angle – value → rotation counterclockwise

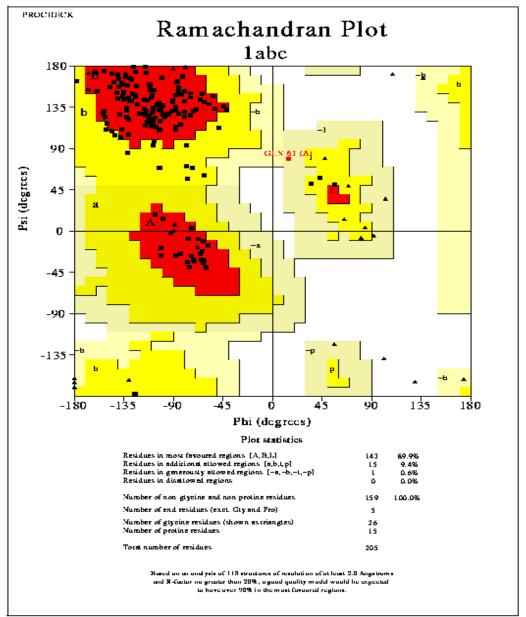


$$C^{\beta}$$
  $C^{\beta}$   $C^{\beta}$   $C^{\beta}$   $C^{\gamma}$  ...  $C^{\alpha}$   $C^{\gamma}$   $C^{\alpha}$   $C^{\gamma}$  ...  $C^{\alpha}$   $C^{\gamma}$   $C^{\alpha}$   $C^{\gamma}$   $C^{\alpha}$   $C^{\gamma}$  ...  $C^{\alpha}$ 



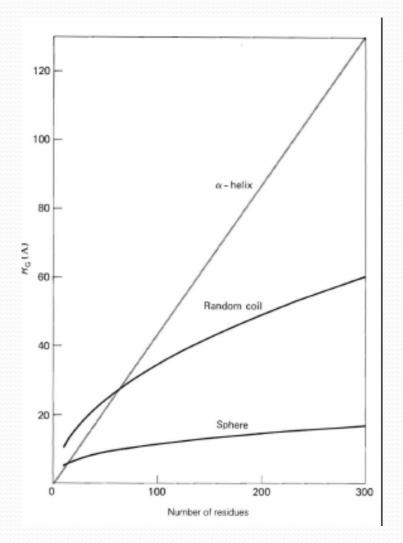
### The Ramachandran Plot

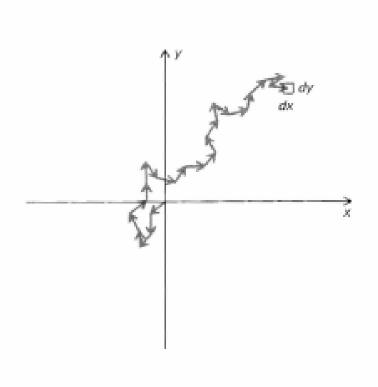


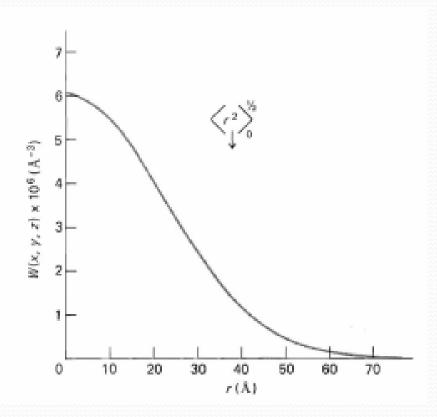


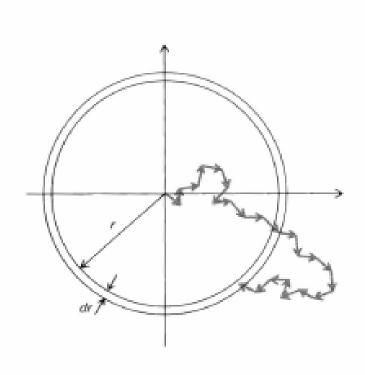
- The intrinsic conformational property of an individual aa makes it possible to calculate the conformational property of a random polymer chain.
- Statistically averaged over all its many possible conformations
- Therefore the unperturbed random coil is the osrt easy to calculate.

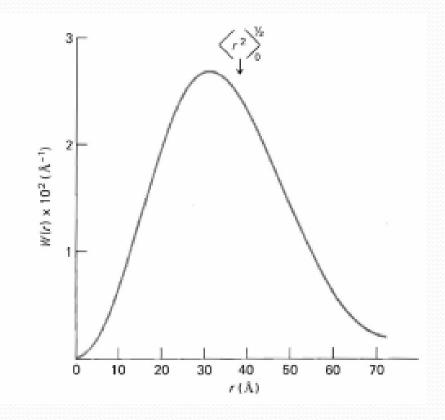
### **End to End Distances**







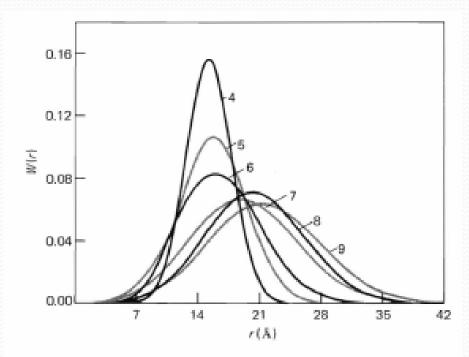




$$W(x, y, z) dx dy dz = (\beta/\sqrt{\pi})^3 e^{-\beta^2 r^2} dx dy dz$$
  
 $W(r) dr = (\beta/\sqrt{\pi})^3 e^{-\beta^2 r^2} 4\pi r^2 dr$ 

$$\begin{array}{c} N(CH_{3})_{2} \\ SO_{2} \\ \hline \\ NH \\ -CH \\ -C \\ (CH_{2})_{2} \\ C \\ -C \\ NH \\ (CH_{2})_{2} \\ -OH \\ \end{bmatrix}_{n}$$

$$-NH-CH-CH_{2}$$
 $C=O$ 
 $NH$ 
 $(CH_{2})_{2}$ 
 $OH$ 
 $(5.12)$ 



#### FIGURE 5.5

Radial distribution function of the distances between naphthalene and dansyl groups attached to the ends of peptides of 4-9 residues of N-hydroxyethyl-Gln, measured by fluorescence energy transfer. (From E. Haas et al., Proc. Natl. Acad. Sci. USA 72:1807-1811, 1975.)

## Transition state theory

$$\Delta S_{\text{conf}} = -b - \frac{3}{2} R \ln n$$

$$v = \frac{k_B T}{h}$$

$$\ln k_{\text{obs}} = \frac{-\Delta H^{\ddagger}}{R} \left( \frac{1}{T} \right) + \frac{\Delta S^{\ddagger}}{R}$$

$$A \stackrel{K^{\ddagger}}{\longleftrightarrow} [A^{\ddagger}] \stackrel{\nu}{\longrightarrow} P \tag{5.15}$$

$$\Delta G^{\ddagger} = -RT \ln K^{\ddagger} = -RT \ln \frac{[A^{\ddagger}]}{[A]}$$
 (5.16)

The kinetic equation for the reaction  $A \rightarrow P$  is then

$$\frac{-d[A]}{dt} = \frac{d[P]}{dt} = k_{\text{obs}}[A] = \frac{k_{\text{B}}T}{h} [A^{\ddagger}] = \frac{k_{\text{B}}T K^{\ddagger}}{h} [A]$$
$$= \frac{k_{\text{B}}T}{h} [A] \exp \frac{-\Delta G^{\ddagger}}{RT}$$
(5.17)

The observed rate constant  $k_{obs}$  is related to the energy of the transition state by

$$k_{\text{obs}} = \frac{k_{\text{B}}T}{h} \exp \frac{-\Delta G^{\ddagger}}{RT}$$
 (5.18)

With the measured value of  $k_{obs}$ , the relative free energy of the hypothetical transition state can be calculated:

$$\Delta G^{\ddagger} = RT \ln \frac{k_{\rm B}T}{k_{\rm obs}h} \tag{5.19}$$

At 25 °C with  $k_{obs}$  expressed in seconds<sup>-1</sup>, this equation has the form

$$\Delta G^{\ddagger} = (17.4 - 1.36 \log k_{\text{obs}}) \text{ kcal/mol} \quad (5.20)$$

#### Intrinsic rates of Bond rotation

Table 5.1 Rotational Relaxation Times in a Random Polypeptide Chain

Carbon a	atom	Relaxation time <sup>a</sup> (10 <sup>-9</sup> s)
Ala	$C^{\beta}$	0.21
Thr	$C^{\beta}$	1.56
	$C^{\gamma}$	0.18
Lys	$C^{\beta}$	0.81
	$C^{\gamma}$	0.54
	$C^{\delta}$	0.60
	C€	0.27
Peptide	$C^{\alpha}$	1.4 - 2.6

<sup>&</sup>lt;sup>a</sup> The values were measured at 45°C on performic acidoxidized ribonuclease A by <sup>13</sup>C nuclear magnetic resonance.

From V. Glushko et al., J. Biol. Chem. 247:3176-3185 (1972).

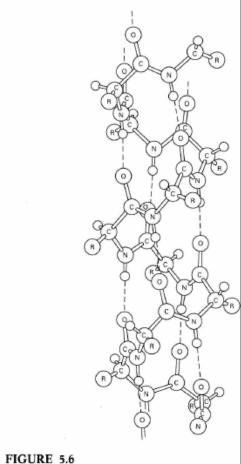
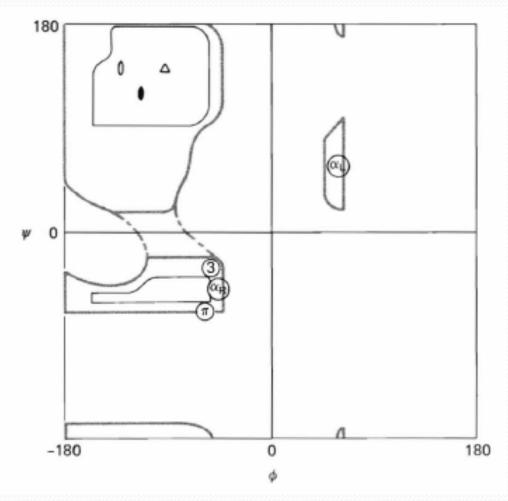


FIGURE 5.6 The classical right-handed  $\alpha$ -helix.

Table 5.2 Parameters for Regular Polypeptide Conformations

	Bond Angle (deg)			Residues	Translation
	φ	Ψ	ω	per turn	per residue (Å)
Antiparallel β-sheet	-139	+135	-178	2.0	3.4
Parallel β-sheet	-119	+113	180	2.0	3.2
Right-handed α-helix	-57	-47	180	3.6	1.50
3 <sub>10</sub> -helix	-49	-26	180	3.0	2.00
π-helix	-57	-70	180	4.4	1.15
Polyproline I	-83	+158	0	3.33	1.9
Polyproline II	-78	+149	180	3.00	3.12
Polyglycine II	-80	+150	180	3.0	3.1

Adapted from G. N. Ramachandran and V. Sasisekharan, *Adv. Protein Chem.* 23:283-437 (1968); IUPAC-IUB Commission on Biochemical Nomenclature, *Biochemistry* 9:3471-3479 (1970).



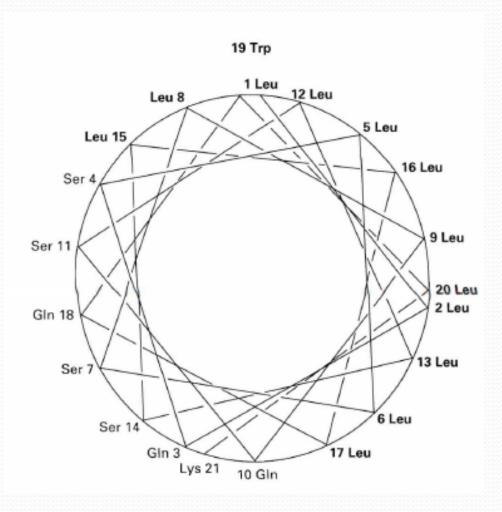


Table 5.3 Relative Helical Tendencies of the Amino Acids Measured in One Peptide

Amino acid residue	Relative stabilization α-helical conformation (kcal/mol)		
Ala	-0.77		
Arg	-0.68		
Lys	-0.65		
Leu	-0.62		
Met	-0.50		
Trp	-0.45		
Phe	-0.41		
Ser	-0.35		
Gln	-0.33		
Glu	-0.27		
Cys	-0.23		
Ile	-0.23		
Tyr	-0.17		
Asp	-0.15		
Val	-0.14		
Thr	-0.11		
Asn	-0.07		
His	-0.06		
Gly	0		
Pro	≈ 3		

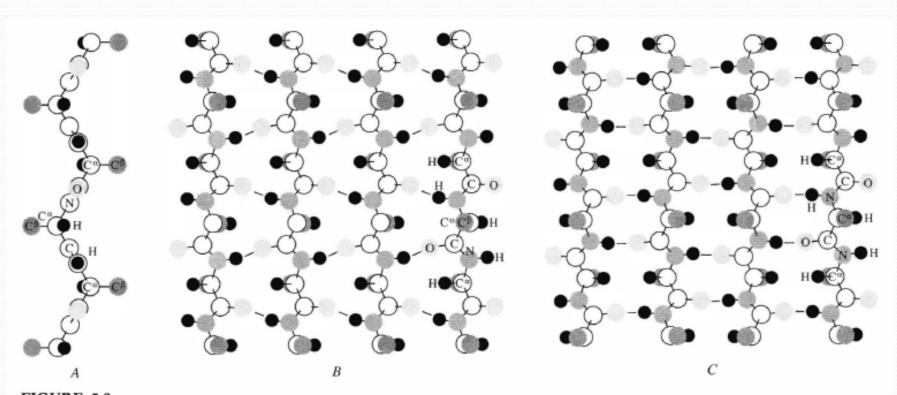
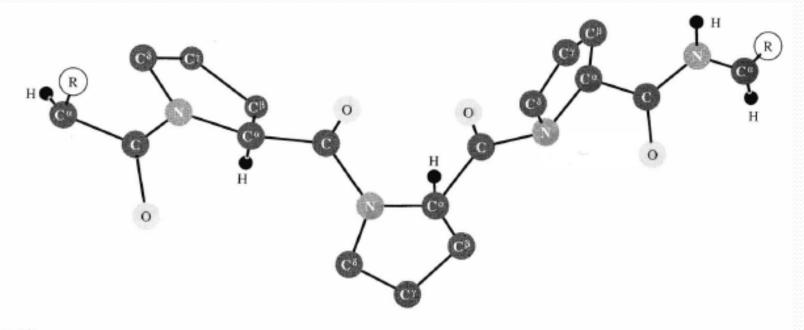
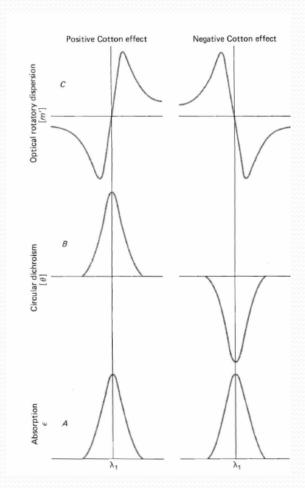


FIGURE 5.9 A single  $\beta$ -strand (A) and its incorporation into flat parallel (B) and antiparallel (C)  $\beta$ -sheets.



#### FIGURE 5.10

The poly(Pro) II helix. (From A. G. Walton, Polypeptides and Protein Structure, Elsevier-North Holland, New York, 1981.)



A typical electronic absorption band (A), which can have either a positive or negative Cotton effect. The two types circular dichroism (B) and optical rotatory dispersion (C) spectra that result are illustrated. (From A. J. Adler et al., Methods Enzymol. 27:675-735, 1973.)

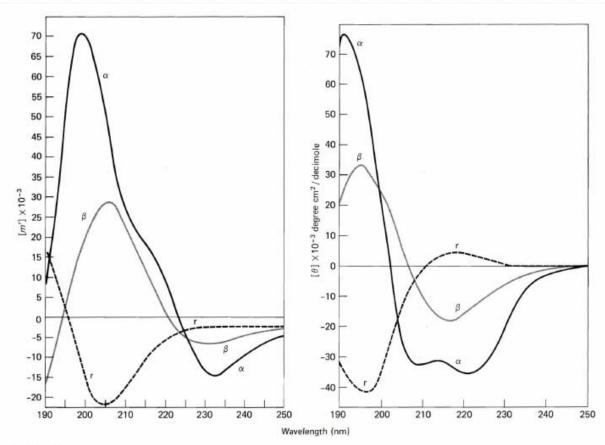
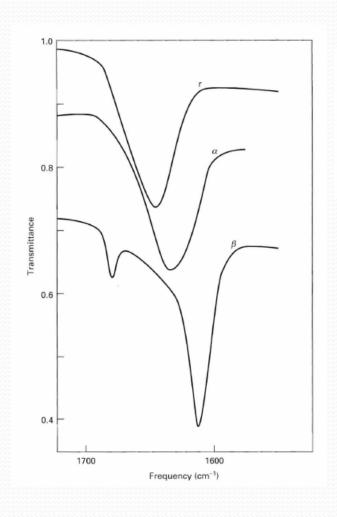


FIGURE 5.12 Optical rotatory dispersion (*left*) and circular dichroism (*right*) spectra of poly(Lys) in the  $\alpha$ -helical ( $\alpha$ ), antiparallel  $\beta$ -sheet ( $\beta$ ), and random-coil (r) conformations. (From N. J. Greenfield et al., *Biochemistry* 6:1630–1637, 1967; 8:4108–4116, 1969.)

Table 5.4 Characteristic Infrared Bands of the Peptide Linkage

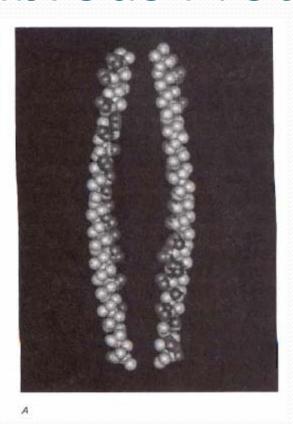
Designation	Approximate frequency (cm <sup>-1</sup> )	Description		
A B	~3300 ~3100	NH stretching in resonance with (2 × amide II) overtone		
I	1600-1690	C=O stretching		
II	1480 - 1575	CN stretching, NH bending		
III	1229-1301	CN stretching, NH bending		
IV	625 - 767	OCN bending, mixed with other modes		
V	640 - 800	Out-of-plane NH bending		
VI	537 - 606	Out-of-plane C=O bending		
VII	~200	Skeletal torsion		

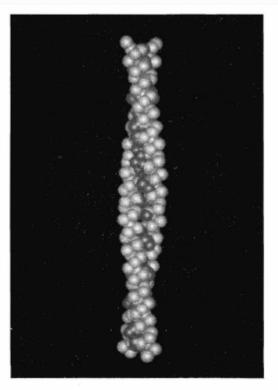
From H. Susi, Methods Enzymol. 26:455-472 (1972).



The amide I band of poly(Lys) in the random coil (r),  $\alpha$ -helix ( $\alpha$ ), and antiparallel  $\beta$ -sheet ( $\beta$ ) conformations, as measured by infrared spectroscopy in  ${}^{2}H_{2}O$ . The characteristic frequencies for this synthetic polyamino acid are somewhat different from those found in other polypeptides and proteins. (From H. Susi, *Methods Enzymol.* 26:455-472, 1972.)

#### Fibrous Proteins

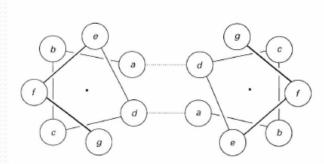


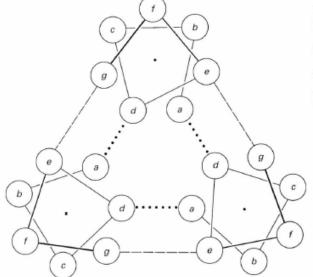


B

The structure of  $\alpha$ -helical coiled coils. A shows two parallel  $\alpha$ -helices twisted slightly as they are when interacting. The shaded atoms make up the apolar stripe of residues a and d of the heptad repeat that pack together in the parallel dimer (B). (From C. Cohen and D. A. D. Parry, *Proteins: Struct. Funct. Genet.* 7:1–15, 1990.)

#### Fibrous Proteins





Helical wheel representations of one heptad repeat of the individual  $\alpha$ -helices, illustrating how the side chains of residues a and d pack together in the two- or three-stranded coiled coils. (From A. C. Steven et al., J. Mol. Biol. 200:351 – 365, 1988.)

#### **Fibrous Proteins**

Table 5.5 Frequency of Occurrence of Amino Acids in the Heptad Repeats of Coiled-Coil Proteins

Amino acid	Average Occurrence at Different Positions (%)						
	а	ь	с	d	e	f	g
Ala	10.2	12.3	8.1	22.2	4.4	11.1	9.3
Cys	0.9	0.0	0.4	0.3	0.2	0.5	0.1
Asp	0.1	13.4	13.0	1.0	4.0	9.8	8.0
Glu	0.8	21.2	19.3	5.5	31.5	14.7	20.1
Phe	2.0	0.4	1.4	2.1	0.4	0.4	0.0
Gly	0.6	1.7	3.5	1.0	1.3	4.2	1.2
His	1.2	2.7	1.6	1.1	0.8	2.6	0.7
Ile	13.2	0.9	2.2	6.3	2.4	2.2	2.2
Lys	7.7	15.3	11.5	0.6	9.0	10.5	14.9
Leu	32.2	1.6	3.9	34.7	6.4	3.9	5.6
Met	4.9	0.9	0.9	2.3	0.9	1.0	0.4
Asn	3.6	4.3	4.6	1.1	5.7	4.8	2.7
Pro	0.0	0.2	0.1	0.0	0.0	0.0	0.0
Gln	0.8	8.7	7.5	4.1	14.0	6.1	13.2
Arg	5.5	6.2	8.2	0.9	6.6	13.2	10.7
Ser	2.1	3.6	8.1	2.2	5.2	8.1	4.5
Thr	1.2	3.8	3.7	2.2	5.1	3.6	3.5
Val	8.9	1.9	1.9	6.0	1.9	3.1	2.7
Trp	0.1	0.0	0.0	0.7	0.0	0.1	0.0
Tyr	4.1	0.9	0.3	5.7	0.3	0.2	0.2

The average occurrences of the various amino acid residues at positions a-b-c-d-e-f-g were tabulated from the heptad repeats of tropomyosin, myosin, paramyosin, and intermediate filament proteins.

From C. Cohen and D. A. D. Parry, Proteins: Struct. Funct. Genet. 7:1-15 (1990).

Model for the three-stranded collagen structure, represented as the repeating sequence -Gly-Pro-γOH Pro-. The three-stranded structure is on the *left*, a single strand on the *right*. (From R. D. B. Fraser et al., *J. Mol. Biol.* 129:463-481, 1979.)

